Janaki. R¹ Dr.Tamilarasi.A²

¹Assistant Professor & Head, Department of Computer Science, N.K.R. Govt. Arts College for Women, Namakkal - 637 001.

> ²Professor & Head, Department of MCA, Kongu Engineering College, Perundurai – 638 052.

Abstract

Image compression is very important for efficient transmission and storage of images. Embedded Zerotree Wavelet (EZW) algorithm is a simple yet powerful algorithm having the property that the bits in the stream are generated in the order of their importance. Image compression can improve the performance of the digital systems by reducing time and cost in image storage and transmission without significant reduction of the image quality. For image compression it is desirable that the selection of transform should reduce the size of resultant data set as compared to source data set. EZW is computationally very fast and among the best image compression algorithm known today. This paper proposes a technique for image compression which uses the Wavelet-based Image Coding. A large number of experimental results are shown that this method saves a lot of bits in transmission, further enhances the compression performance. This paper aims to determine the best threshold to compress the still image at a particular decomposition level by using Embedded Zero-tree Wavelet encoder. Compression Ratio (CR) and Peak-Signal-to-Noise (PSNR) is determined for different threshold values ranging from 6 to 60 for decomposition level 8.

Keywords

Image Compression, Embedded Zero-tree Wavelet (EZW), Zero-tree.

1.Introduction

Wavelet based image compression techniques are increasingly used for image compression. The wavelet based coding divides the image into different subbands.[1] These sub-bands can then be successively quantized using different quantizers to give better compression. The wavelet filters are so designed that the coefficients in each sub-band are almost uncorrelated with each other. The basic objective of image compression is to find an image representation in which pixels are less correlated. The two fundamental principles used in image compression are redundancy and irrelevancy. Redundancy removes redundancy from the signal source and irrelevancy omits pixel values which are not noticeable by human eye. The basic objective of image compression is to find an image representation in which pixels are less correlated. It reduces the number of bits needed to represent an image by removing the spatial and spectral redundancies. Discrete wavelet transform (DWT) [2] become a cutting edge technology in image data compression. Image compression is typically comprised of three basic steps. Firstly, the image is transformed into wavelet coefficients which are then quantized in a quantizer and finally thresholded which makes the coefficient smaller than a chosen threshold value (zero) obtained from the quantizer. As a result, some bits are reduced producing an output bit stream.

1.1 Need for image compression

The need for image compression becomes apparent when number of bits per image are computed resulting from typical sampling rates and quantization methods. For example, the amount of storage required for given images is (i) a low resolution, TV quality, color video image which has 512 x 512 pixels/color, 8 bits/pixel, and 3 colors approximately consists of 6×10^6 bits;(ii) a 24 x 36 mm negative photograph scanned at 12 x 10⁻⁶mm:3000 x 2000 pixels/color, 8 bits/pixel, and 3 colors nearly contains 144 x 10⁶ bits; (3) a 14 x 17 inch radiograph scanned at 70 x 10⁻⁶mm: 5000 x 6000 pixels, 12 bits/pixel nearly contains 360 x 10⁶ bits[3]

1.2 Principles behind compression

Number of bits required to represent the information in an image can be minimized by removing the redundancy present in it. There are three types of redundancies: (i) spatial redundancy, which is due to the correlation or dependence between neighbouring pixel values; (ii) spectral redundancy, which is due to the correlation between different color planes or spectral bands; (iii) temporal redundancy, which is present because of correlation between different frames in images .Image compression research aims to reduce the number of bits required to represent an image by removing the spatial and spectral redundancies as much as possible[4].

This paper contributes to the implementation of EZW algorithm in which approximated and detailed components are further decomposed if the sum of information content is less than the information content of component which has been decomposed[5].

The main contribution of EZW encoding is that it visually improves the compression of an image by increasing the decomposition level 8.

2. EZW Encoding

The EZW encoder was originally designed to operate on images (2D-signals) but it can also be used on other dimensional signals. It is based on progressive encoding to compress an image into a bit stream with increasing accuracy [5]. This means that when more bits are added to the stream, the decoded image will contain more detail, a property similar to JPEG encoded images. Using an embedded coding algorithm, an encoder can terminate the encoding at any point thereby allowing a target rate or target accuracy to be met exactly. The EZW algorithm is based on four key concepts: 1) a discrete wavelet transform or hierarchical sub band decomposition, 2) prediction of the absence of significant formation across scales by exploiting the self-similarity inherent in images, 3) entropy-coded successive approximation quantization, and 4) universal lossless data compression which is achieved via entropy encoding[6,7].

The EZW encoder is based on two important observations:

1. Natural images in general have a low pass spectrum. When an image is wavelet transformed the energy in the sub bands decreases as the scale decreases (low scale means high resolution), so the wavelet coefficients will, on average, be smaller in the higher sub bands than in the lower sub bands. This shows that progressive encoding is a very natural choice for compressing wavelet transformed images, since the higher sub bands only add detail[9,10].

2. Large wavelet coefficients are more important than small wavelet coefficients.

These two observations are exploited by encoding the wavelet coefficients in decreasing order, in several passes. For every pass a threshold is chosen against which all the wavelet coefficients are measured. If a wavelet coefficient is larger than the threshold it is encoded and removed from the image, if it is smaller it is left for the next pass. When all the wavelet coefficients have been visited the threshold is lowered and the image is scanned again to add more detail to the already encoded image. This process is repeated until all the wavelet coefficients have been encoded[6].

2.1 Concept of Zero-tree

A wavelet transform transforms a signal from the time domain to the joint time-scale domain. i.e. the wavelet coefficients are two-dimensional. To compress the transformed signal not only the coefficient values, but also their position in time has to be coded. When the signal is an image then the position in time is better expressed as the position in space. After wavelet transforming an image it can be represented using trees because of the sub sampling that is performed in the transform. A coefficient in a lower sub band can be thought of as having four descendants in the next higher sub band as shown in Fig.2.1 The four descendants each also have four descendants in the next higher sub band, which gives a quad-tree, with every root having four leafs.

A zero tree is defined as a quad-tree of which all nodes are equal to or smaller than the root and the root is smaller than the threshold against which the wavelet coefficients are currently being measured. The tree is coded with a single symbol and reconstructed by the decoder as a quad-tree filled with zeroes[11]. The EZW encoder codes the zero tree based on the observation that wavelet coefficients decrease with scale. In a zero tree all the coefficients in a quad tree are smaller than the threshold if the root is smaller than this threshold. Under this case the whole tree can be coded with a single zero tree (T) symbol[8].

A scanning of the coefficient is performed in such a way that no child node is scanned before its parent. For an N scale transform, the scan begins at the lowest frequency sub band, denoted as LLN, and scans sub bands HLN, LHN, and HHN, at which point it moves on to scale N-1 etc.[11] The two such scanning patterns

for a three-scale pyramid can be seen in Fig. 2.1. Note that each coefficient within a given sub band is scanned

before any coefficient in the next sub band.

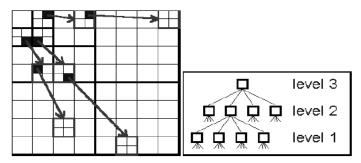


Fig 2.1 The relation between wavelet coefficients in sub bands as quad tree

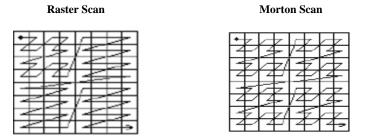


Fig 2.2 Different scanning patterns for scanning wavelet coefficients

Given a threshold level T to determine whether a coefficient is significant, a coefficient x is said to be an element of a zero tree for threshold T if itself and all of its descendents are insignificant with respect to T. An element of a zero tree for threshold T is a zero tree root if it is not the descendents of a previously found zero tree root for threshold T, i.e., it is not predictably insignificant from the discovery of a zero tree root at a coarser scale at the same threshold[12].

A zero tree root is encoded with a special symbol indicating that the insignificance of the coefficient at finer scales is completely predictable. The significance map can be efficiently represented as a string of symbols from a 3-symbol alphabet which is then entropy encoded.

3. Implementation

Coding the wavelet coefficients is performed by determining two lists of coefficients:

1. The dominant list D contains information concerning significance of coefficients.

2. The significant list S contains the amplitude values of the significant coefficients.

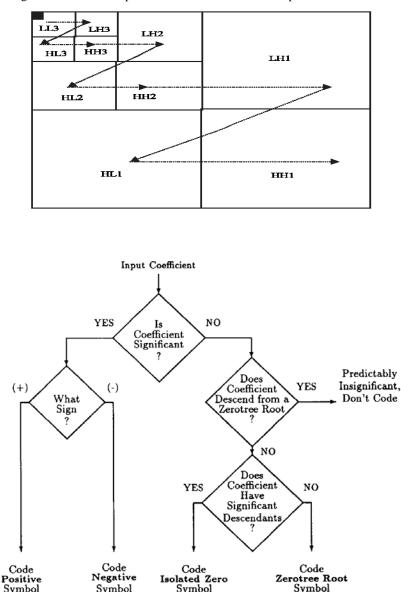
| 63 | -34 | 49 | 10 | 7 | -13 | 12 | 7 |
|-----|-----|-----|-----|---|-----|----|---|
| -31 | 23 | -14 | -13 | 3 | 4 | 6 | 1 |
| 15 | 14 | 3 | -12 | 5 | -7 | 3 | 9 |
| -9 | -7 | -14 | 8 | 4 | -2 | 3 | 9 |
| -5 | 9 | -1 | 47 | 4 | -6 | -2 | 2 |
| 3 | 0 | -3 | 2 | 2 | -2 | 0 | 4 |
| 2 | -3 | 6 | 4 | 3 | 6 | 3 | 6 |
| 5 | 11 | 5 | 6 | 0 | 3 | -4 | 4 |

Fig.3.1 Example of decomposition to three resolution for an 8*8 matrix

Significance test :

The wavelet transform coefficients are scanned for the path as shown in the fig below. In our implemented

method, we have used Mortan scan, which is more accurate and produces standard results.



Flow chart for encoding a co-efficient of the significance map

EZW coding algorithm:

Each coefficient is assigned a significance symbols (P, N, Z, T), by comparing with the actual threshold.

- 1. P (significance and positive): if the absolute value of the coefficient is higher than the threshold T and is positive.
- 2. N (significance and positive): if the absolute value of the coefficient is higher than the threshold T and is negative.
- 3. T (zerotree): if the value of the coefficient is lower than the threshold T and has only insignificant descendants

4. Z (isolated zero): if the absolute value of the coefficient is lower than the threshold T and has one or more significant descendents.

The insignificant coefficients of the last sub bands, which do not accept descendents and are not themselves descendents of a zerotree, are also considered to be zero tree.



The dominant list and the significance list are shown below:

D: P N Z T P T T T T T Z T T T T T T T P T T

S: 1010

| 5 | In | the | dominant | list | since | the | probability | of |
|------------|-----|-----|----------|------|-------|-----|-------------|----|
| <i>J</i> • | 111 | unc | aommuni | mou | Shice | unc | probubility | 01 |

| Parameter | TH=6 | TH=10 | TH=30 | TH=60 | |
|-----------------|--------|---------|--------|--------|--|
| | | | | | |
| Original File | 65240 | 65240 | 65240 | 65240 | |
| Size(bytes) | 03240 | 03240 | 03240 | 03240 | |
| | | | | | |
| Compressed File | 11107 | 10070 | 0044 | 0427 | |
| Size (bytes) | 11186 | 10870 | 9944 | 8437 | |
| | | | | | |
| Compression | 5.83 | 6.00 | 6.56 | 7.73 | |
| Ratio (CR) | 5.85 | 0.00 | 0.30 | 1.15 | |
| | | | | | |
| Bits Per Pixel | 2.52 | 1.48 | 0.7087 | 0.3145 | |
| (Bpp) | 2.32 | 1.40 | 0.7087 | 0.3143 | |
| | | | | | |
| Peak-Signal-to- | | | | | |
| Noise Ratio | 34.362 | 34.1648 | 33.672 | 32.330 | |
| | 54.502 | 54.1046 | 55.072 | 52.550 | |
| (PSNR) | | | | | |
| | | | | | |

occurrence of the symbol T is more when

compared to others, this symbol should be coded with the less number of bits.

6. After encoding all the symbols with binary digits, a separator is appended to the end of the encoded bit stream to indicate the end of the stream.

For eg:

In our algorithm to encode the symbols P, N, Z and T we use the binary bits as follows:

P is encoded as 1110

N is encoded as 110

Z is encoded as 10

since the probability of occurrence is less when compared to T.

T is encoded as 0 (since the probability of occurrence is more when compared to other bits)

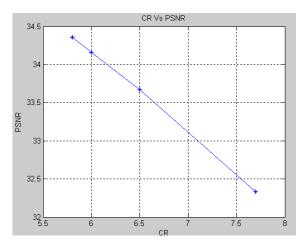
Then we insert a separator bits i.e. a stream of 1's . Here we used 11111 to indicate the end of the bit stream.

For decoding from the encoded bit stream the dominant list symbols are found and from these symbols the pixels values of the image are predicted.

4. Results

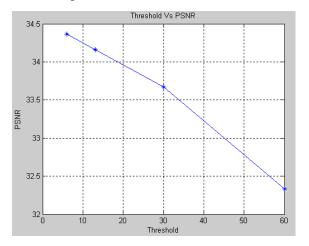
Firstly, original image is applied to the compression program, EZW encoded image is obtained. To reconstruct compressed image, compressed image is applied to decompression program, by which EZW decoded image is obtained. Compression Ratio (CR) and Peak-Signal-to-Noise Ratio (PSNR) are obtained for the original and reconstructed images. In the experiment the original image 'Lena.tif' having size 256×256 (65,536 Bytes). The different statistical values of the image Lena.tif for Various Thresholds are summarized in the table.

Thus, it can be concluded that EZW encoding gives excellent results. By choosing suitable threshold value compression ratio as high as 8 can be achieved.

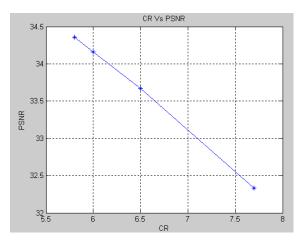


4.1 (a) CR Vs PSNR





4.1 (b) THR Vs PSNR



4.1 (c) CR Vs PSNR

The curves of CR Vs PSNR , THR Vs PSNR and CR Vs PSNR have been calculated and depicted in the fig 4.1 (a), (b) & (c) respectively. In which Image encoded using EZW algorithm for 8 level decomposition gives better BPP and PSNR values.

5. Conclusion

In this paper the Embedded Zero-tree Wavelet coding scheme was implemented. The effect of using different Wavelet transforms, using different block sizes and different bit rates were studied. This approach utilizes zero tree structure of wavelet coefficients at decomposition level 8 is very effectively, which results in higher compression ratio and better PSNR. The algorithm is tested on different images, and it is seen that the results obtained by Image encoded using EZW algorithm is better than other methods.

Threshold=10







Threshold=60





6. References

- V.S. Shingate, T. R. Sontakke & S.N. Talbar, "Still Image Compression using Embedded Zerotree Wavelet Encoding", International Journal of Computer Science & Communication", Vol. 1, No. 1, January-June 2010, pp.21-24
- [2] Marcus J. Nadenau, Julien Reichel and Murat Kunt, "Visually Improved Image Compression by Combining a conventional Wavelet-Codec with Texture Modeling," IEEE Transactions on Image Processing, Vol. 11, No. 11, Nov 2002, pp. 1284-1294.
- [3] Rafael C. Gonzalez, Richared E. Woods, Steven L.Eddins, Digital Image Proceeding Using MATLAB, 2008, Pearson Education
- [4] K. Sayood, Introduction to Data Compression, 2nd Ed, 2000 Academic Press, Morgan Kaufmann publishers.
- [5] Shapiro, J. M., Embedded Image Coding Using Zerotrees of Wavelet Cefficients, IEEE Transactions on Signal Processing, 41, No. 12 (1993), p. 3445-3462.
- [6] Kharate G.K., Ghatol A. A. and Rege P. P., " Image Compression Using Wavelet Packet Tree," ICGST-GVIP.
- [7] S. D. Servetto, K. Ramchandran, and M. T. Orchard, "Image coding based on a morphological representation of wavelet data", IEEE Trans. Image Processing, vol. 8, pp. 1161-1174, Sept. 1999.
- [8] Vinay U. Kale & Nikkoo N. Khalsa,International Journal of Computer Science & Communication "Performance Evaluation of Various Wavelets for Image Compression of Natural and Artificial Images",Vol. 1, No. 1, January-June 2010, pp. 179-184,
- [9] Tripatjot Singh, Sanjeev Chopra, Harmanpreet Kaur, Amandeep Kaur,Image Compression Using Wavelet and Wavelet Packet Transformation,IJCST Vol.1, Issue 1, September 2010.
- [10] Uytterhoeven G., "Wavelets: Software and Applications", U. Leuven Celestijnenlaan, Department of Computer Science, Belgium, 1999.

- [11] Jerome M. Shapiro," Embedded Image Coding Using Zerotrees of Wavelet Coefficients," IEEE Transactions on Signal Processing, December 1993.
- [12] Lotfi A. A., Hazrati M. M., Sharei M., Saeb Azhang, "Wavelet Lossy Image Compression on Primitive FPGA", IEEE, pp. 445-448, 2005.

